

Joint Transmit Power and Placement Optimization for URLLC-Enabled UAV Relay Systems

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Abstract—This letter considers an unmanned aerial vehicle (UAV)-enabled relay communication system for delivering latency-critical messages with ultra-high reliability, where the relay is operating under amplifier-and-forward (AF) mode. We aim to jointly optimize the UAV location and power to minimize decoding error probability while guaranteeing the latency constraints. Both the free-space channel model and three-dimensional (3-D) channel model are considered. For the first model, we propose a low-complexity iterative algorithm to solve the problem, while globally optimal solution is derived for the case when the signal-to-noise ratio (SNR) is extremely high. For the second model, we also propose a low-complexity iterative algorithm to solve the problem. Simulation results confirm the performance advantages of our proposed algorithms.

Index Terms—UAV, URLLC, short-packet transmission, relay.

I. INTRODUCTION

Recently, unmanned aerial vehicle (UAV) communication has received considerable research interests due to its flexible deployment and the dominance of line-of-sight links [1], [2]. UAV can be deployed as a relay when there is no direct link between any two nodes. Specifically, Zeng *et al.* [3] first studied the trajectory and power allocation for UAV-relay systems. In [4], the reliability of the UAV relay was analyzed in terms of outage probability and bit error rate.

On the other hand, ultra-reliable and low-latency communications (URLLC) have been regarded as one of the three important use cases in 5G [5]. For URLLC, a transmitter usually sends a short packet such as command signals or measurement data to a receiver, in contrast to conventional human-to-human communication where long packet is normally transmitted. Hence, a direct result of the Shannon's capacity based on the law of large numbers may not be applicable. In [6], Peter *et al.* have derived the maximal coding rate for short-packet transmission, which is a complicated function of channel blocklength and SNR.

In this paper, we consider a two-dimensional UAV-enabled industrial automation scenario in Fig. 1, where a controller needs to send command messages to a distant robot that conducts an experiment

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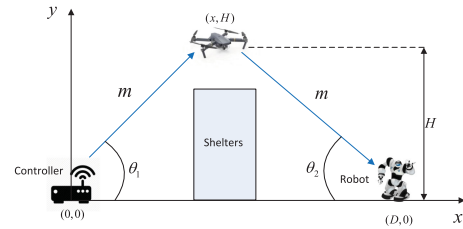


Fig. 1. UAV relay system for delivering URLLC services.

in a multi-hazard area. For the safety of workers, shelters such as thick cement/metal walls are built between the robot and the controller. Hence, the channel gain between the controller and the robot is weak and negligible, and requires a UAV to fly above the shelter to assist the transmission between the controller and the robot. In [7], we studied the problem of jointly optimizing the blocklength and location for UAV-relay communication systems, where the decoding-and-forward (DF) protocol was considered. However, additional processing time is required for the DF mode, which may not be applicable to URLLC applications. Motivated by above, we jointly optimize power and location to minimize the decoding error probability, where the relay is operating under the AF mode without the signal processing delay. The decoding error probability under short blocklength is adopted. We first prove that the decoding error probability is a monotonically decreasing function the SNR. Then, two channel models are studied: free-space channel model and the 3-D channel model. For the first one, an iterative algorithm is proposed to obtain the suboptimal solution with low complexity, and the globally optimal solution is obtained in closed form when the SNR is extremely high. Simulation results show the performance advantages of our proposed algorithms.

II. SYSTEM MODEL

As shown in Fig. 1, we consider a two-dimensional UAV-enabled industrial automation scenario, where the UAV hovers at a location (x, H) above the horizontal line with height H . The locations of the controller and the robot are $(0, 0)$ and $(D, 0)$. The packet size of the command information is L bits, which should be completed within T_{\max} seconds. Then, the overall blocklength is given by $M = BT_{\max}$ [8], where B is system bandwidth. The total transmission has two phases, i.e., the first one corresponds to the transmission from the controller to the UAV, while the second one is the transmission from the UAV to the robot. We assume that the UAV adopts the AF protocol, which simply amplifies and forwards the received signals to the robot. Hence, the blocklength for these two phases should be equal, e.g., $m_1 = m_2 = m \triangleq M/2$. The transmit power of the controller and the UAV are respectively p_1 and p_2 .

The channel power gain from the controller to the UAV and from the UAV to the robot are denoted as h_1 and h_2 , respectively. These channel gains depends on the height H and horizontal distance x . In the first phase, the received signal at UAV is given by $y_1 = \sqrt{p_1 h_1} x_1 + n_1$, where x_1 is the command signal transmitted by the controller with unit power, and n_1 is the received noise at the UAV that is normalized to unit. The amplification coefficient at the UAV is given by $G = \sqrt{p_2 / (p_1 h_1 + 1)}$. In the second phase, the received signal at the robot is given by $y_2 = \sqrt{h_1 h_2 p_1 G} x_1 + \sqrt{h_2 G} n_1 + n_2$, where n_2 is the noise power at the robot that is normalized to unit. Then, the

received signal-to-noise ratio (SNR) at the robot is

$$\gamma = \frac{h_1 h_2 p_1 p_2}{h_2 p_2 + h_1 p_1 + 1}. \quad (1)$$

In [6], the packet error probability of the AF relay system in short blocklength region can be approximately as:

$$\varepsilon = Q(f(\gamma, m, L)), \quad (2)$$

where $f(\gamma, m, L) = \ln 2 \sqrt{\frac{m}{V(\gamma)}} (\log_2(1 + \gamma) - \frac{L}{m})$, $V(\gamma)$ is the channel dispersion given by $V(\gamma) = 1 - (1 + \gamma)^{-2}$ [6], and $Q(x)$ is the Gaussian Q -function.

In this paper, we aim to minimize ε by optimizing the power allocation and the location of the UAV:

$$\min_{\{p_1, p_2, x, H\}} \varepsilon \quad (3a)$$

$$\text{s.t.} \quad d_1 \leq x \leq d_2, \quad (3b)$$

$$H_{\min} \leq H \leq H_{\max}, \quad (3c)$$

$$p_1 + p_2 \leq P_T, \quad (3d)$$

$$p_1 \geq 0, p_2 \geq 0, \quad (3e)$$

where constraint (3b) and (3c) specifies the feasible flying region of the UAV, and P_T is the total power limit.

Before solving Problem (3), we first provide the following lemmas.

Lemma 1: The packet decoding error probability ε is a decreasing function of SNR γ .

Proof: This can be proved by carefully checking the sign of the first-order derivative of the decoding error probability with respect to SNR. Details are omitted due to page limit. ■

Then, Problem (3) can be equivalently formulated as

$$\max_{\{p_1, p_2, x, H\}} \gamma \quad (4a)$$

$$\text{s.t.} \quad (3b), (3c), (3d), (3e). \quad (4b)$$

Then, we have the following lemma.

Lemma 2: The total power constraint in (3d) holds with equality at the optimal solution.

Proof: This can be proved by using contradiction, the details of which are omitted due to limited space. ■

It is difficult to obtain the globally optimal solution of Problem (4) because the power allocation are coupled with the location. In the following, we first consider the free-space channel model, and then we consider the more practical 3-D channel model.

III. FREE-SPACE CHANNEL MODEL

In this section, we assume the channel is dominated by line-of-sight (LOS) component, and consider the free space channel model, i.e.,

$$h_1 = \frac{\beta_1}{H^2 + x^2}, \quad h_2 = \frac{\beta_2}{H^2 + (D - x)^2}, \quad (5)$$

where β_1 and β_2 are channel power gains at a reference distance of $d = 1$ meter for the two links, respectively. In this case, we fix the height H , and optimize the power and horizontal distance x . Then, Problem (4) becomes

$$\max_{\{p_1, p_2, x\}} \gamma \quad (6a)$$

$$\text{s.t.} \quad (3b), (3d), (3e). \quad (6b)$$

In the following, we first consider the general case and solve the problem by using the block coordinate decent (BCD) method. Then, we consider the special case when the SNR is extremely high, where the globally optimal solution can be obtained.

A. General Case-BCD Method

In the following, we decouple Problem (6) into two subproblems, i.e., optimize power allocation with fixed x and vice versa. Then, iteratively solve these two subproblems until convergence.

1) *Power Allocation With Fixed x :* Given x , Problem (4) can be transformed to the following subproblem:

$$\max_{\{p_1, p_2\}} \gamma \quad (7a)$$

$$\text{s.t.} \quad (3d), (3e). \quad (7b)$$

By substituting $p_2 = P_T - p_1$ into the expression of γ in (1) and performing some manipulations, γ can be rewritten as:

$$\gamma = -\frac{h_1 h_2}{A^2} (A p_1 + B) - \frac{h_1 h_2 B}{A} \left(\frac{B}{A} + P_T \right) + \frac{h_1 h_2}{A} \left(\frac{2B}{A} + P_T \right),$$

where $A = h_1 - h_2$ and $B = P_T h_2 + 1$. The second order derivative of γ w.r.t. p_1 is calculated as

$$\frac{\partial^2 \gamma}{\partial p_1^2} = -\frac{2h_1 h_2 B (B + A P_T)}{(A p_1 + B)^3}$$

which can be checked to be negative. Hence, γ is a concave function and the optimal solution of Problem (7) can be derived as follows:

$$p_1^* = \frac{\sqrt{B(B + A P_T)} - B}{A}, \quad p_2^* = P_T - p_1^*. \quad (8)$$

2) *Location Optimization With Fixed p_1 and p_2 :* By substituting the expressions of h_1 and h_2 in (5) into the expressions of γ , Problem (4) is equivalent to

$$\min_x p_2 \beta_2 D_1(x) + p_1 \beta_1 D_2(x) + D_1(x) D_2(x) \quad (9a)$$

$$\text{s.t.} \quad d_1 \leq x \leq d_2, \quad (9b)$$

where $D_1(x) = H^2 + x^2$ and $D_2(x) = H^2 + (D - x)^2$. Obviously, the objective function (OF) in Problem (9) is a continuous function, and the globally optimal solution of Problem (9) is among the locally optimal solutions and boundary points. By setting the first derivative of OF w.r.t. x to zero, we have

$$ax^3 + bx^2 + cx + d = 0, \quad (10)$$

where $a = 4$, $b = -6D$, $d = -2(DH^2 + D p_1 \beta_1)$, and $c = 2(D^2 + 2H^2 + \beta_1 p_1 + \beta_2 p_2)$. Dividing equation (10) by a and substituting $x = t - b/3a$, we have

$$t^3 + \rho t + \kappa = 0, \quad (11)$$

where $\rho = \frac{3ac - b^2}{3a^2}$ and $\kappa = \frac{2b^3 - 9abc + 27a^2 d}{27a^3}$.

Equality (11) is a cubic equation. The equation may have only one real solution or three solutions, which depends on the conditions. Specifically, if $4\rho^3 + 27\kappa^2 > 0$ and $\rho < 0$, there is only one real solution, given by

$$t_0 = -2 \frac{|\kappa|}{\kappa} \sqrt{-\frac{\rho}{3}} \cosh \left(\frac{1}{3} \operatorname{arccosh} \left(\frac{-3|\kappa|}{2\rho} \sqrt{\frac{-3}{\rho}} \right) \right), \quad (12)$$

if $\rho > 0$, there is only one real solution, given by

$$t_0 = -2\sqrt{\frac{\rho}{3}} \sinh\left(\frac{1}{3} \operatorname{arsinh}\left(\frac{3\kappa}{2\rho} \sqrt{\frac{3}{\rho}}\right)\right), \quad (13)$$

otherwise, there are three real solutions given by

$$t_k = 2\sqrt{-\frac{\rho}{3}} \cos\left(\frac{1}{3} \arccos\left(\frac{3\kappa}{2\rho} \sqrt{\frac{-3}{\rho}}\right) - \frac{2\pi k}{3}\right), \quad k = 0, 1, 2. \quad (14)$$

Once obtaining the real solution of (11), set $x_0 = t_0 - b/3a$ for only one real solution, and $x_k = t_k - b/3a$, $k = 0, 1, 2$ for three different real solutions. For the one real solution case, if x_0 is in the range of $[d_1, d_2]$, choose one from the set $\{d_1, d_2, x_0\}$ with the minimum OF of Problem (9), otherwise, choose one from set $\{d_1, d_2\}$ with the best OF. For the three real solutions case, choose the solutions that fall within the range of $[d_1, d_2]$, which is denoted as S . Then, choose the one from the set $\{d_1, d_2, S\}$ with the best OF as the globally optimal solution.

Finally, the BCD method, which iterates between power allocation and location optimization, is applied to solve Problem (4) for the general case. The details are omitted for simplicity.

B. Special Case: $1 \ll h_i p_i, i = 1, 2$

In this case, the SNR γ can be approximated as

$$\gamma \approx \frac{h_1 h_2 p_1 p_2}{h_2 p_2 + h_1 p_1} \triangleq \tilde{\gamma}. \quad (15)$$

By substituting the expressions of h_1 and h_2 in (5) into (15), $\tilde{\gamma}$ can be obtained as

$$\tilde{\gamma} = \frac{\beta_1 \beta_2 p_1 p_2}{\beta_2 p_2 (H^2 + x^2) + \beta_1 p_1 (H^2 + (D - x)^2)}. \quad (16)$$

Let us denote $x_0 = \frac{D\beta_1 p_1}{\beta_1 p_1 + \beta_2 p_2}$. The optimal x that maximizes $\tilde{\gamma}$ can be expressed as

$$x^* = \begin{cases} x_0, & \text{if } d_1 \leq x_0 \leq d_2, \\ d_1, & \text{if } x_0 \leq d_1, \\ d_2, & \text{if } x_0 \geq d_2. \end{cases} \quad (17)$$

We consider the conditions in (17) case-by-case.

1) *Condition I:* $d_1 \leq x_0 \leq d_2$: By substituting the optimal $x^* = x_0$ into (16), Problem (4) can be rewritten as

$$\min_{\{p_1 \geq 0, p_2 \geq 0\}} \frac{H^2 (\beta_1 p_1 + \beta_2 p_2)}{p_1 p_2} + \frac{\beta_1 \beta_2 D^2}{\beta_1 p_1 + \beta_2 p_2} \quad (18a)$$

$$\text{s.t.} \quad D\beta_1 p_1 \geq \beta_1 d_1 p_1 + \beta_2 d_1 p_2, \quad (18b)$$

$$D\beta_1 p_1 \leq \beta_1 d_2 p_1 + \beta_2 d_2 p_2, \quad (18c)$$

$$p_1 + p_2 = P_T, \quad (18d)$$

where (18d) is due to Lemma 2.

In the following, we address Problem (18) by considering two cases:

1) $\beta_1 = \beta_2$; 2) $\beta_1 \neq \beta_2$.

Case I: $\beta_1 = \beta_2$: Problem (18) is equivalent to

$$\max_{p_1 \geq 0} p_1 (P_T - p_1) \quad (19a)$$

$$\text{s.t.} \quad \frac{d_2 P_T}{D} \geq p_1 \geq \frac{d_1 P_T}{D}. \quad (19b)$$

Obviously, the optimal solution can be obtained as follows:

$$p_1^* = \begin{cases} \frac{d_2 P_T}{D}, & \text{if } 2d_2 \leq D, \\ \frac{d_1 P_T}{D}, & \text{if } 2d_1 \geq D, \\ \frac{P_T}{2}, & \text{otherwise.} \end{cases} \quad (20)$$

Then, the optimal p_2 is given by $p_2^* = P_T - p_1^*$.

Case II: $\beta_1 \neq \beta_2$: The closed-form solution cannot be obtained as Case I. However, we can obtain the globally optimal solution of Problem (18).

Theorem 1: Problem (18) is a convex optimization problem.

Proof: Obviously, the set of constraints in Problem (18) is linear. Hence, we only need to prove the convexity of the OF of Problem (18).

Denote OF of Problem (18) as function $f(p_1, p_2)$. Obviously, $f(p_1, p_2)$ is twice differentiable, and its Hessian matrix can be derived as

$$\nabla^2 f = \begin{bmatrix} \frac{2H^2\beta_2}{p_1^3} + \frac{2\beta_1^3\beta_2 D^2}{(\beta_1 p_1 + \beta_2 p_2)^3} & \frac{2\beta_1^2\beta_2^2 D^2}{(\beta_1 p_1 + \beta_2 p_2)^3} \\ \frac{2\beta_1^2\beta_2^2 D^2}{(\beta_1 p_1 + \beta_2 p_2)^3} & \frac{2H^2\beta_1}{p_2^3} + \frac{2\beta_1\beta_2^3 D^2}{(\beta_1 p_1 + \beta_2 p_2)^3} \end{bmatrix} \quad (21)$$

and its determinant is checked to be strictly bigger than zero. In addition, both the diagonal elements are strictly positive. Hence, $\nabla^2 f$ is positive definite. The proof completes. ■

The globally optimal solution can be obtained by using standard convex optimization algorithms such as interior-point method [9].

2) *Condition II:* $x_0 < d_1$: By substituting $x^* = d_1$ into (16) and using Lemma 2, Problem (4) can be rewritten as

$$\max_{p_1} \frac{\beta_1 \beta_2 p_1 (P_T - p_1)}{(\beta_1 D_2 - \beta_2 D_1) p_1 + \beta_2 D_1 P_T} \quad (22a)$$

$$\text{s.t.} \quad 0 \leq p_1 \leq p_1^{\text{up}}, \quad (22b)$$

where $D_1 = H^2 + d_1^2$, $D_2 = H^2 + (D - d_1)^2$, and $p_1^{\text{up}} = \frac{d_1 \beta_2 P_T}{(D - d_1) \beta_1 + d_1 \beta_2}$.

We solve this problem by considering two cases: 1) $\beta_1 D_2 = \beta_2 D_1$; 2) $\beta_1 D_2 \neq \beta_2 D_1$.

Case I: $\beta_1 D_2 = \beta_2 D_1$: The optimal solution of Problem (22) can be obtained as follows:

$$p_1^* = \begin{cases} \frac{P_T}{2}, & \text{if } p_1^{\text{up}} > \frac{P_T}{2} \\ p_1^{\text{up}}, & \text{otherwise.} \end{cases} \quad (23)$$

Case II: $\beta_1 D_2 \neq \beta_2 D_1$: The OF of Problem (22) can be rewritten as:

$$\tilde{\gamma} = \frac{\beta_1 \beta_2}{\beta_1 D_2 - \beta_2 D_1} \left(-(p_1 + E) - \frac{E(E + P_T)}{p_1 + E} + 2E + P_T \right),$$

where E is equal to $\frac{\beta_2 D_1 P_T}{\beta_1 D_2 - \beta_2 D_1}$. The second derivative of $\tilde{\gamma}$ w.r.t. p_1 is given by

$$\frac{\partial^2 \tilde{\gamma}}{\partial p_1^2} = -\frac{2\beta_1 \beta_2}{\beta_1 D_2 - \beta_2 D_1} \frac{E(E + P_T)}{(p_1 + E)^3} \quad (24)$$

which is proved to be negative. Hence, Problem (22) is a convex optimization problem. Define $\bar{p}_1 \triangleq \sqrt{E(E + P_T)} - E$. The optimal solution is given by

$$p_1^* = \begin{cases} \bar{p}_1, & \text{if } p_1^{\text{up}} > \bar{p}_1 \\ p_1^{\text{up}}, & \text{otherwise.} \end{cases} \quad (25)$$

3) *Condition III:* $x_0 > d_2$: The optimal solution in this case can be obtained by using the similar method as those in Condition II, the details of which are omitted here.

When the optimal solution for each condition is obtained, select one solution with the largest value of $\tilde{\gamma}$ as the globally optimal solution of Problem (4).

IV. 3-D CHANNEL MODEL

In this section, we extend the free-space channel model to 3-D channel model proposed in [10], where the impacts of blockage and shadowing are taken into account and is more practical than free-space channel model. In specific, the line-of-sight (LoS) probability is given by

$$P_{\text{LoS}} = \frac{1}{1 + a \exp(-b(\theta - a))}, \quad (26)$$

where a and b are positive environment-related parameters and θ is the elevation angle between the UAV and the ground devices (controller or robot) as shown in Fig. 1. Some typical values of a and b can be found in Table I of [11]. It is observed from (26) that the LoS probability increases with the elevation angle, which is reasonable as the probability that signal is blocked is decreasing when the height of UAV is increasing.

When the location of one UAV is given, the mean path loss is given by [10]:

$$L(\theta, d) = \frac{A}{1 + a \exp(-b(\theta - a))} + 20\log_{10}(d) + C, \quad (27)$$

where A and C are constants given by $A = \eta_{\text{LoS}} - \eta_{\text{NLoS}}$ and $C = 20\log_{10}(\frac{4\pi f_c}{c}) + \eta_{\text{NLoS}}$, respectively. d is the distance between the UAV and the ground devices (controller or robot). η_{LoS} and η_{NLoS} are the path loss (in dB) corresponding to the LoS and non-LoS (NLoS) links. In general, η_{NLoS} is larger than η_{LoS} due to the more severe attenuation associated with NLoS. f_c is the central frequency point, c is the light speed.

Based on the path loss model in (27), the normalized channel gains w.r.t. noise power are given by

$$h_i = \tilde{C}_i d_i^{-2} 10^{\frac{\tilde{A}_i}{1 + a_i \exp(-b_i(\theta_i - a_i))}}, \quad i = 1, 2 \quad (28)$$

where $\tilde{A}_i = -\frac{A_i}{10} > 0$ and $\tilde{C}_i = 10^{-\frac{C_i}{10}} / \delta^2$ with δ^2 denoting the noise power, and θ_i are given by

$$\theta_1 = \arctan\left(\frac{H}{x}\right), \theta_2 = \arctan\left(\frac{H}{D-x}\right). \quad (29)$$

Similar to the free-space case, we also adopt the BCD algorithm to solve Problem (4). When x and H are given, channel gains h_1 and h_2 are fixed. Then, the power allocation can be optimized by using the same method in Subsection III-A1. In the following, we only focus on the optimization of height H and horizontal distance x when the other parameters are fixed.

A. Optimization of H With Fixed x , p_1 and p_2

When x , p_1 and p_2 are given, the SNR $\gamma(H)$ is a very complicated function of H . It is difficult to strictly prove the monotonically and convexity of this function. As in [11] and [7], we graphically illustrate these properties in Fig. 2, where we show the SINR $\gamma(H)$ versus H with $x = 100$ m. Four different scenarios are illustrated, and the corresponding parameters for each scenario are given in [11]. It can be found from this figure that for each scenario, the SINR value first increases with height H and then decreases with H . As a result, there exists only one maximum point for each scenario, denoted as H^* . The value of H^* is the solution to the following equation:

$$\frac{d\gamma(H)}{dH} = 0. \quad (30)$$

Similar to [11], the bisection search method can be used to find the root of the above equation.

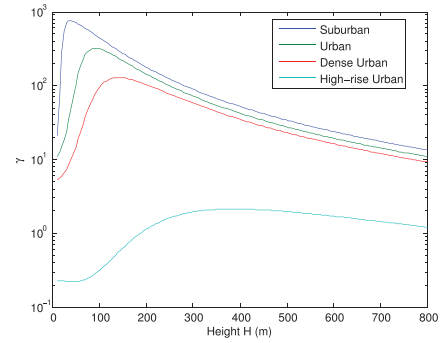


Fig. 2. SINR γ versus height H when $x = 100$ m.

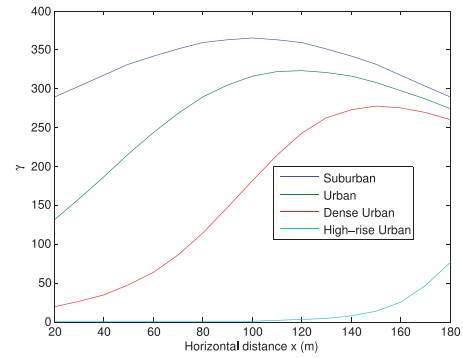


Fig. 3. SINR γ versus the horizontal distance x when $H = 120$ m.

B. Optimization of x With Fixed H , p_1 and p_2

In Fig. 3, we illustrate the SINR value versus the horizontal distance x when $H = 120$ m. The channel from the controller the UAV is assumed to be suburban environment. The SNR values when the channel from the UAV to the robot experiences various environments are shown in Fig. 3. Similar to Fig. 2, the SINR value also first increases with x and then decreases with x , or always increases with x . Then, the bisection search method can be adopted to find the optimal solution.

V. SIMULATION RESULTS

Simulation results are performed to check the performance of the proposed algorithms. The system parameters are set as $D = 200$ m, $H = 120$ m, $d_1 = 30$ m, $d_2 = 170$ m, $L = 100$ bits, $M = 80$, and $P_T = 4$ Watt.

A. Free-Space Channel Model

We first study the free-space channel model, where $\beta_1 = 50$ dB, $\beta_2 = 59$ dB.

In Fig. 4, we study the convergence behaviour of the iterative algorithm for the general case. It is shown that the proposed iterative algorithm converges rapidly and in general four iterations are sufficient for the algorithm to converge, which implies low complexity of our proposed algorithm.

In Fig. 5, we compare the performance of various algorithms, which include: 1) General case ('General-Case Alg. '); 2) High-SNR case ('High-SNR Alg. '); 3) Exhaustive search algorithm ('Exhaustive Search '); 4) Fixed location with $x = (d_1 + d_2)/2$ ('Fixed-Loca. '); 5) Fixed power allocation with $p_1 = p_2 = P_T/2$ ('Fixed-Power '). We also compare the proposed algorithm for AF relay with the one for DF relay in [7]. For the DF relay, the number of channel uses for the signal

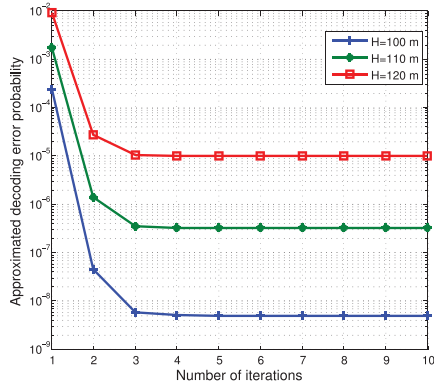
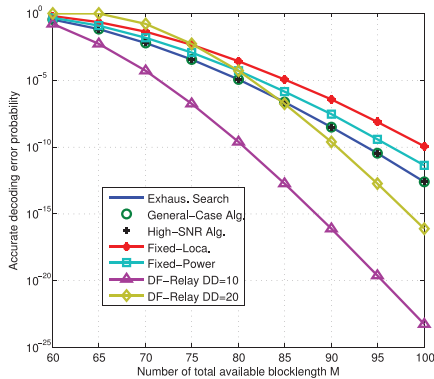


Fig. 4. Convergence behaviour.

Fig. 5. Performance comparison, $H = 120$ m.

processing at the relay is denoted as DD.¹ It is observed in Fig. 5 that the proposed two algorithms significantly outperform the Fixed-LoCa algorithm and Fixed-Power algorithm, which confirms the benefits of our proposed algorithms. It is interesting to find that the proposed two algorithms have almost the same performance as the exhaustive search method. This may be due to the fact that the SNR in this example generally operates in a very high regime. When the signal processing delay DD is small (e.g. DD = 10), the DF relay outperforms the AF relay, which means DF relay is a good option. On the other hand, when DD is large, the AF relay performs better than the DF relay when the number of channel blocklength M is small. In this example, when DD=20, the performance of the AF relay is better than that of the DF relay when $M \leq 85$. This means that it is beneficial to adopt the AF relay when the latency requirement is stringent, which is usually the case in URLLC applications. The reason is that when more time is used for signal processing, the left time for data transmission will be reduced, which decreases the reliability performance.

B. 3-D Channel Model

In Fig. 6, we study the performance of the algorithm developed in Section IV for the 3-D channel model. The simulation parameters are set as follows: $H_{\min} = 10$ m, $H_{\max} = 200$ m, $d_1 = 20$ m, $d_2 = 200$ m, $f_c = 2.5$ GHz, noise power is -93 dB. The channel model from the controller the UAV is assumed to be suburban environment. We study the performance when the channel from the UAV to the robot experiences various environments. The environment parameters are referred to [11]. To study the importance of optimizing the height, we

¹In general, the system bandwidth is fixed, and then the number of channel users can be interpreted as time duration.

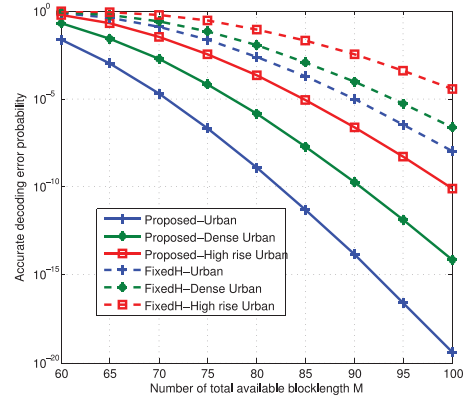


Fig. 6. Performance comparison for 3-D channel models.

also show the performance when the height is fixed as $H = 100$ m, which is denoted as ‘FixedH’ in Fig. 6. It can be observed that the proposed joint optimization algorithm outperforms the ‘FixedH’ algorithm for various environments, and the performance gains increase with M , which confirms the importance of optimizing the height.

VI. CONCLUSION

This paper studied the joint power allocation and location optimization for UAV AF-relay system with URLLC requirements. Both the free-space channel and the 3-D channel are considered. For the free-space channel, the iterative algorithm was proposed for general case, and the closed-form solution was derived for the special case with high SNR. A low-complexity iterative algorithm was proposed for the 3-D channel model. Simulation results showed that the proposed algorithms can achieve the same performance as the exhaustive search method, and outperform the other algorithms such as fixed location or fixed power allocation.

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